

The Use of Decision Trees for Adaptive Item Selection and Score Estimation

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Why Not Standard CAT?

- Not all measures or indices conform to an IRT model, which is often the basis of CAT
 - Example: network size
- IRT-based item banks are expensive to develop and maintain, and require specialized skills

Purpose

- Provide an overview of decision tree methods
- Compare the use of decision tree approaches to IRT-based CAT using instruments consisting of dichotomous and polytomous items.

Decision Trees

- A decision tree predicts membership on an outcome based on one or more predictor variables.
- Predictors are used to partition the sample into subsamples that are increasingly homogeneous on the outcome.
- Each subsample is represented by a node in the tree structure.
- The partitioning process is repeated until a stopping rule is met

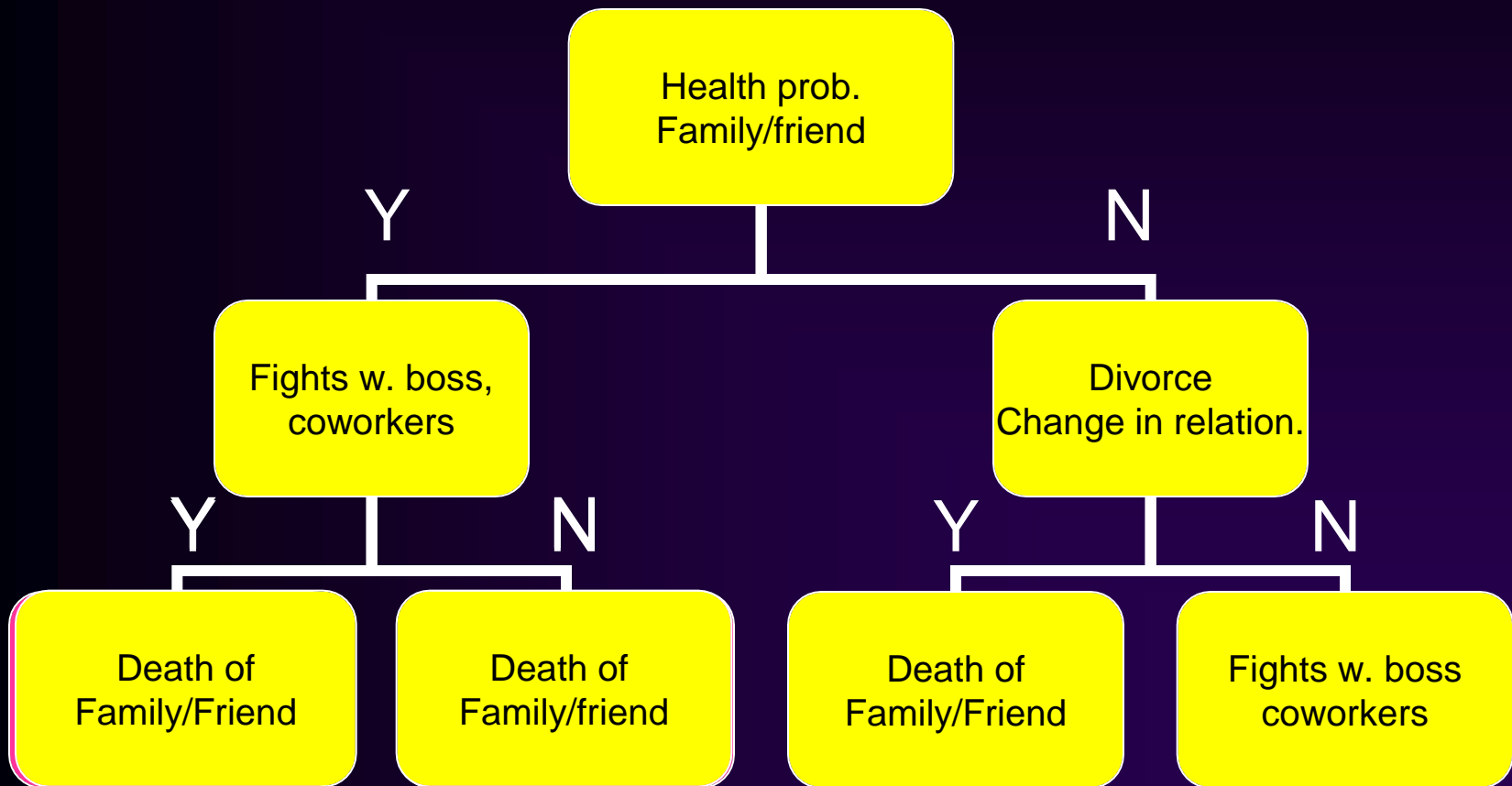
Decision Trees cont.

- Stopping criterion can be based on:
 - Number of levels or depth of the tree
 - A minimum sample size for a given node
- Terminal nodes (nodes at the lowest level of the tree)
 - associated with an estimated probability of being in a particular category on the outcome variable
 - in the case of interval-level outcomes, a mean value on that variable.

Partitioning Algorithms

- Regression trees
 - Similar to ANOVA and discriminant analysis and generally used to predict a continuous outcome
 - Nodes are divided into 2 sub nodes
- CHAID – chi-square automatic interaction detection
 - Used to predict a categorical outcome
 - Nodes can be divided into two or more sub nodes.

Example: Personal Sources of Stress



Decision Tree Pros and Cons

- Pros
 - Does not require assumptions of unidimensionality or local independence
 - Can handle item non-response more easily than CAT
 - Less computationally intensive during administration
 - Can incorporate demographic variables to control “DIF”
- Cons
 - Error propagation: A wrong decision (item) can lead to all subsequent decisions being wrong as well.

Study

- Conducted post-hoc simulations comparing the relative efficiency, and precision of decision trees (using CHAID and CART) vs. IRT-based CAT.
- Measure: Global Appraisal of Individual Needs (GAIN) Substance Problem Scale (16 items)
 - Past-year symptom count (SPSy)
 - Recency of symptom scale (SPSr)

Data Source

- Data from 26,390 participants entering substance abuse treatment
- Dataset was split into two random samples
 - The first sample was used for development of the decision-tree models and for IRT parameter estimation
 - The second sample was used to compare CAT vs. decision-tree efficiency and precision.
- IRT model
 - 2 parameter dichotomous model (SPSy)
 - 2 parameter graded response model (SPSr)

Stop Rule Criterion

- Decision Trees
 - Maximum number of levels (4-10)
 - No nodes w. $N < 100$ and no new nodes created w. a parent node of $N < 200$
- CAT
 - Maximum number of items
 - Standard error of measurement $< .4475$
(measure reliability = .80)

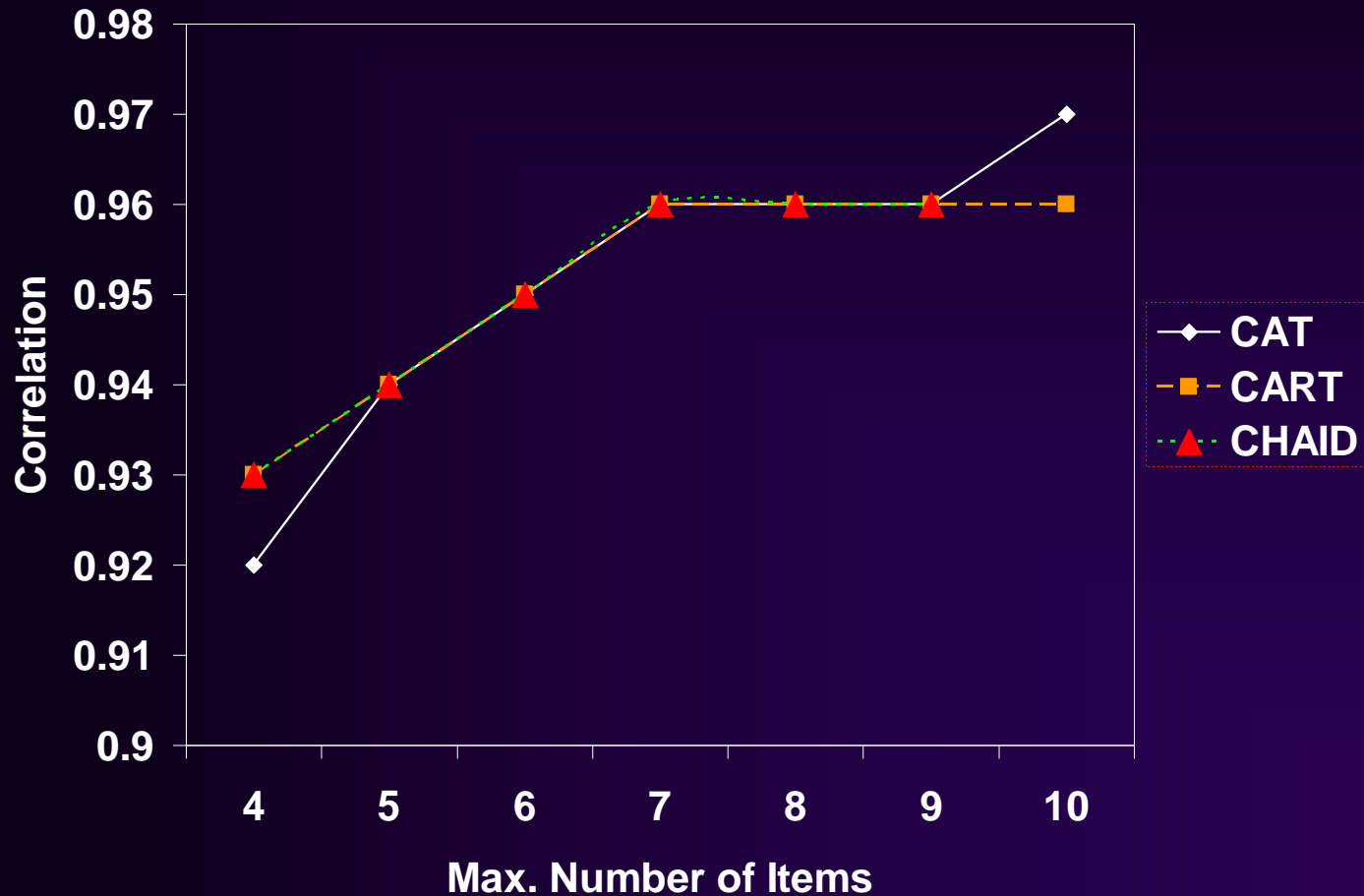
Procedures

- Decision-tree models were developed using SPSS (v. 19).
- Mplus (v. 6) was used to estimate IRT item parameters
- CAT simulations used maximum Fisher's information and were performed using Firestar version 1.33
- Since the decision tree models were used to estimate raw scores, raw score equivalents of IRT measures were used for comparison.

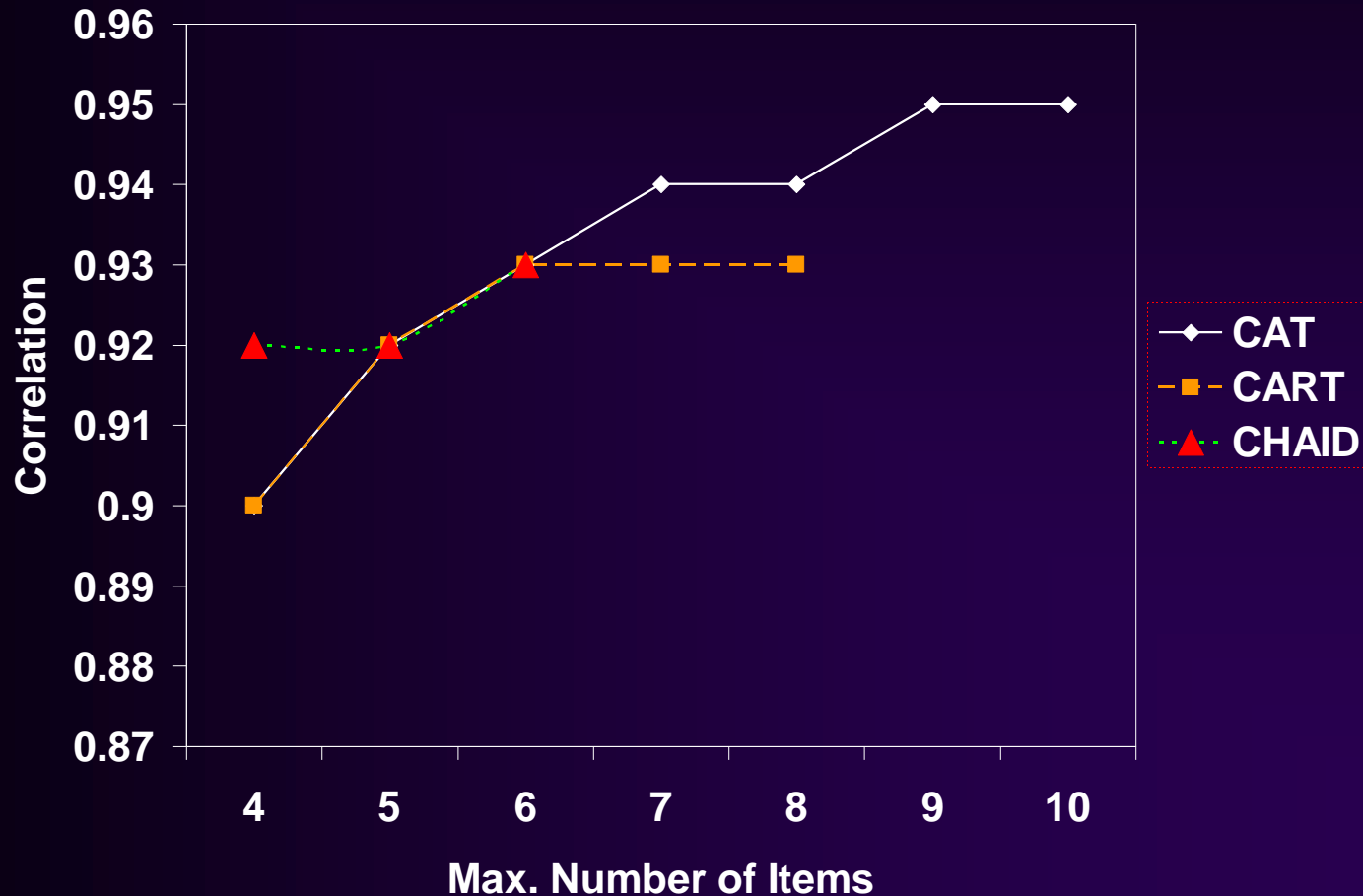
Comparison Criteria

- Correlation w. Total Score (R)
- Efficiency (R^2 x % items saved)
- Bias (Mean CAT/Tree vs. Mean Full)
- Root Mean Squared Error (RMSE)
difference between estimated and full scores
- Effect Size (Comparison between persons in outpatient vs. residential treatment)

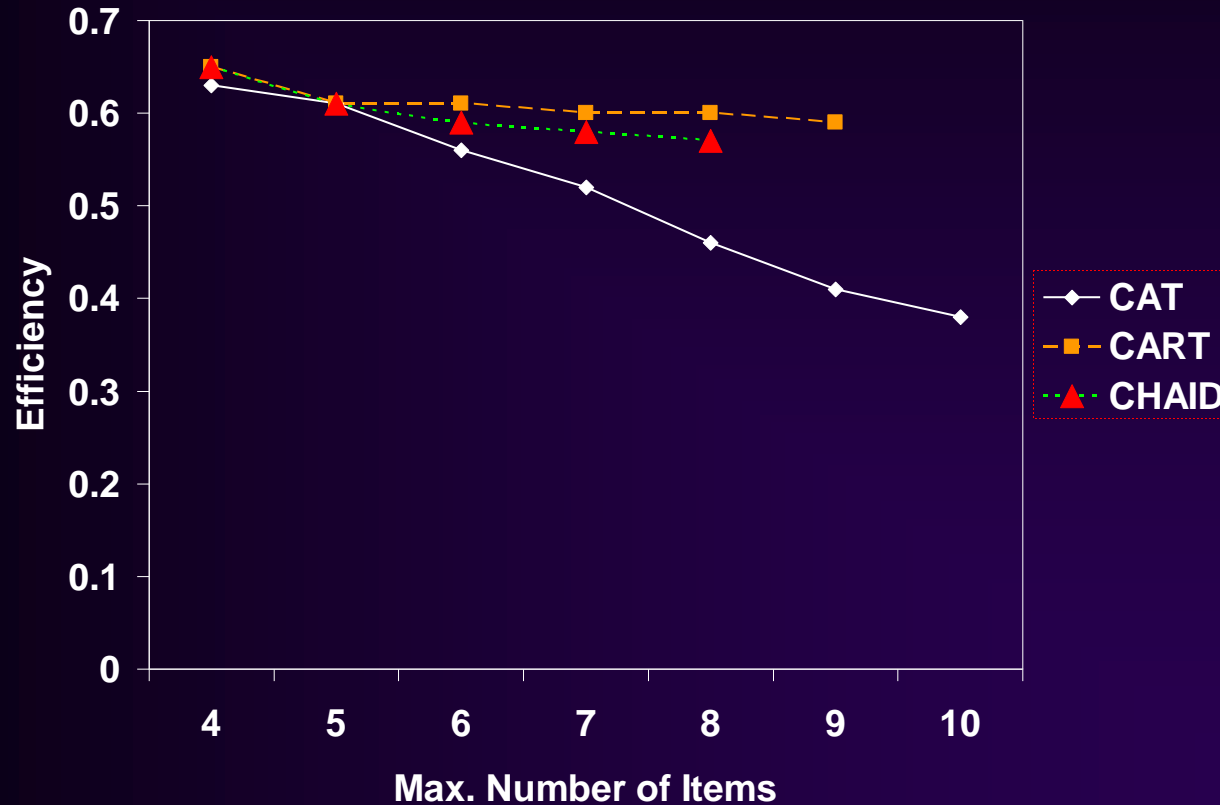
SPSy: Corr. With Total Score



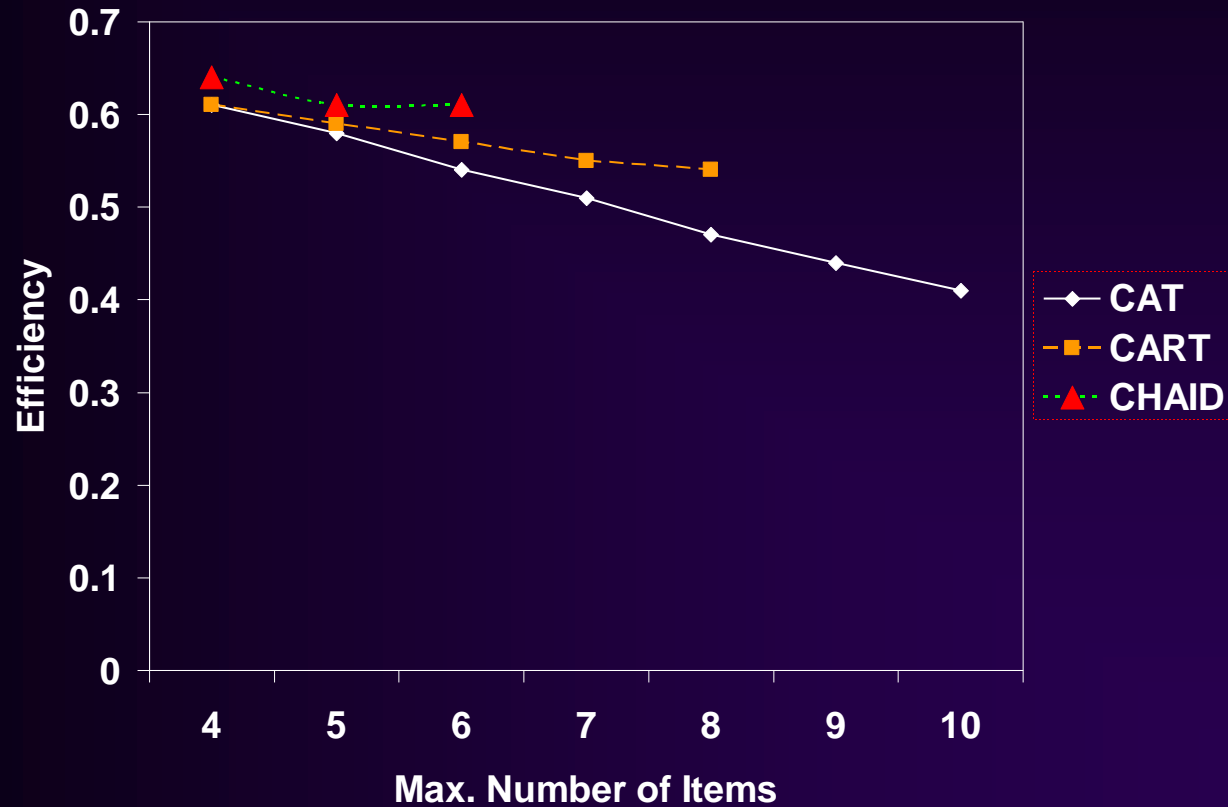
SPSr: Corr. w. Total Score



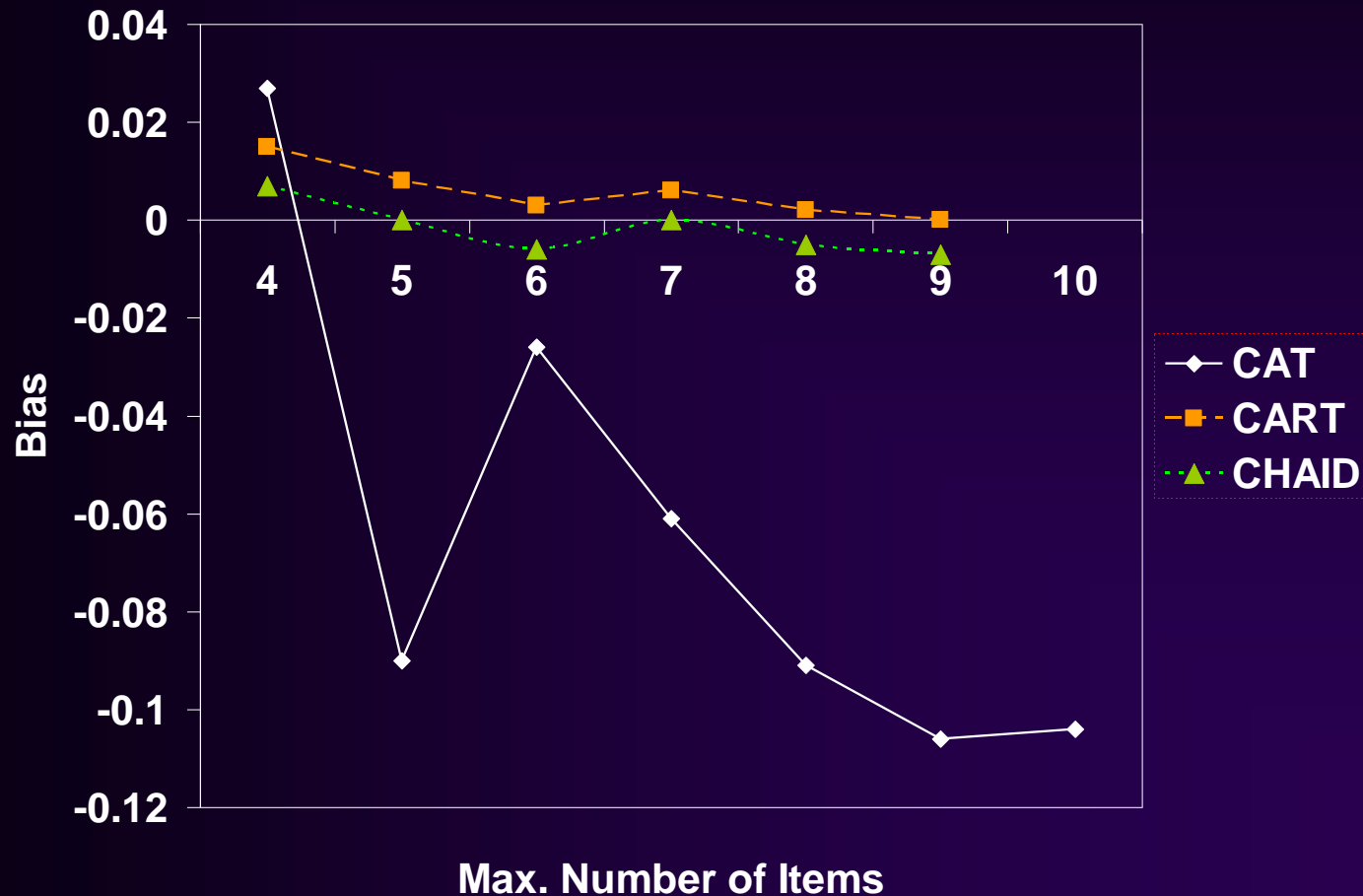
SPSy: Efficiency



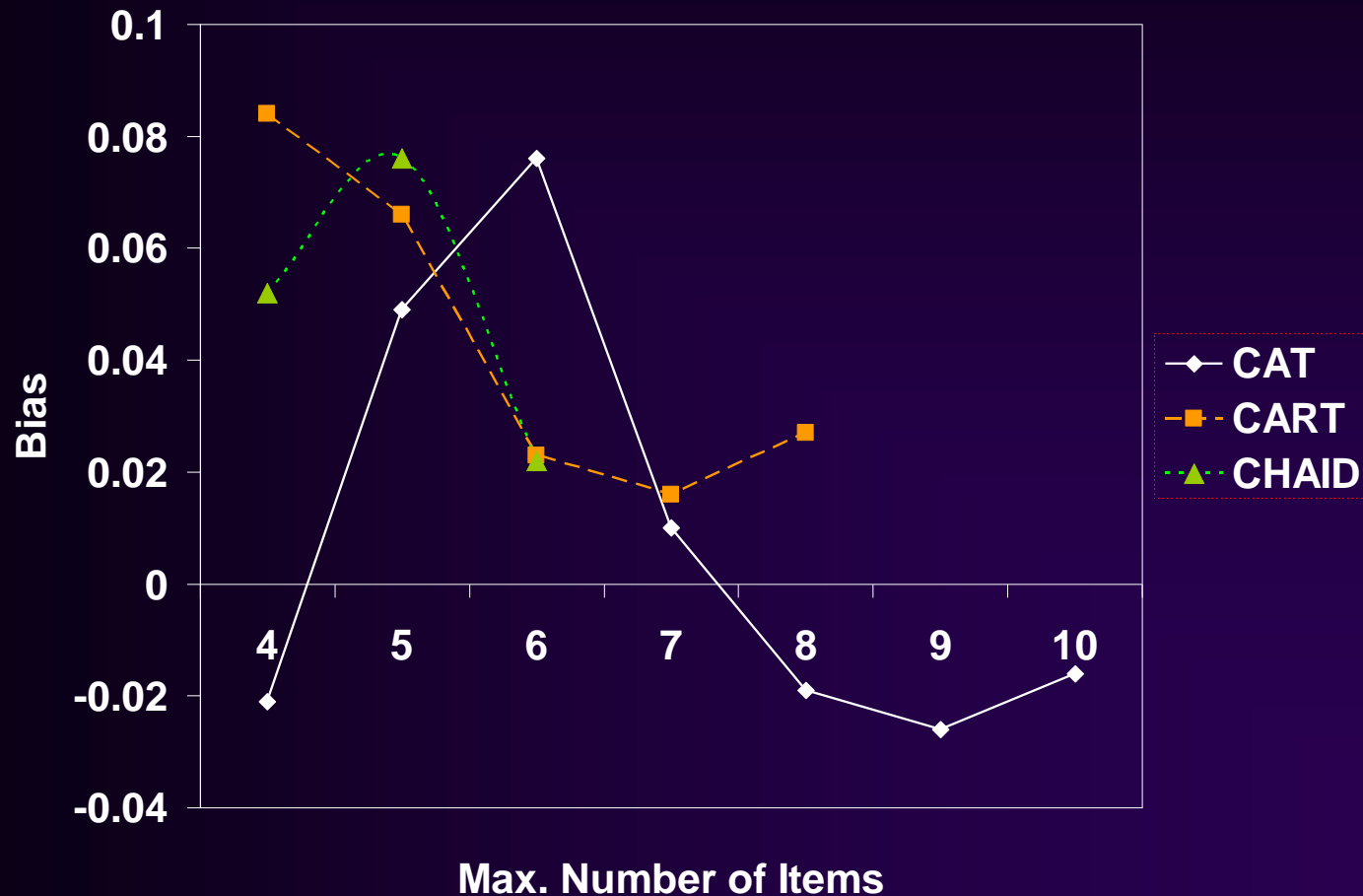
SPSr: Efficiency



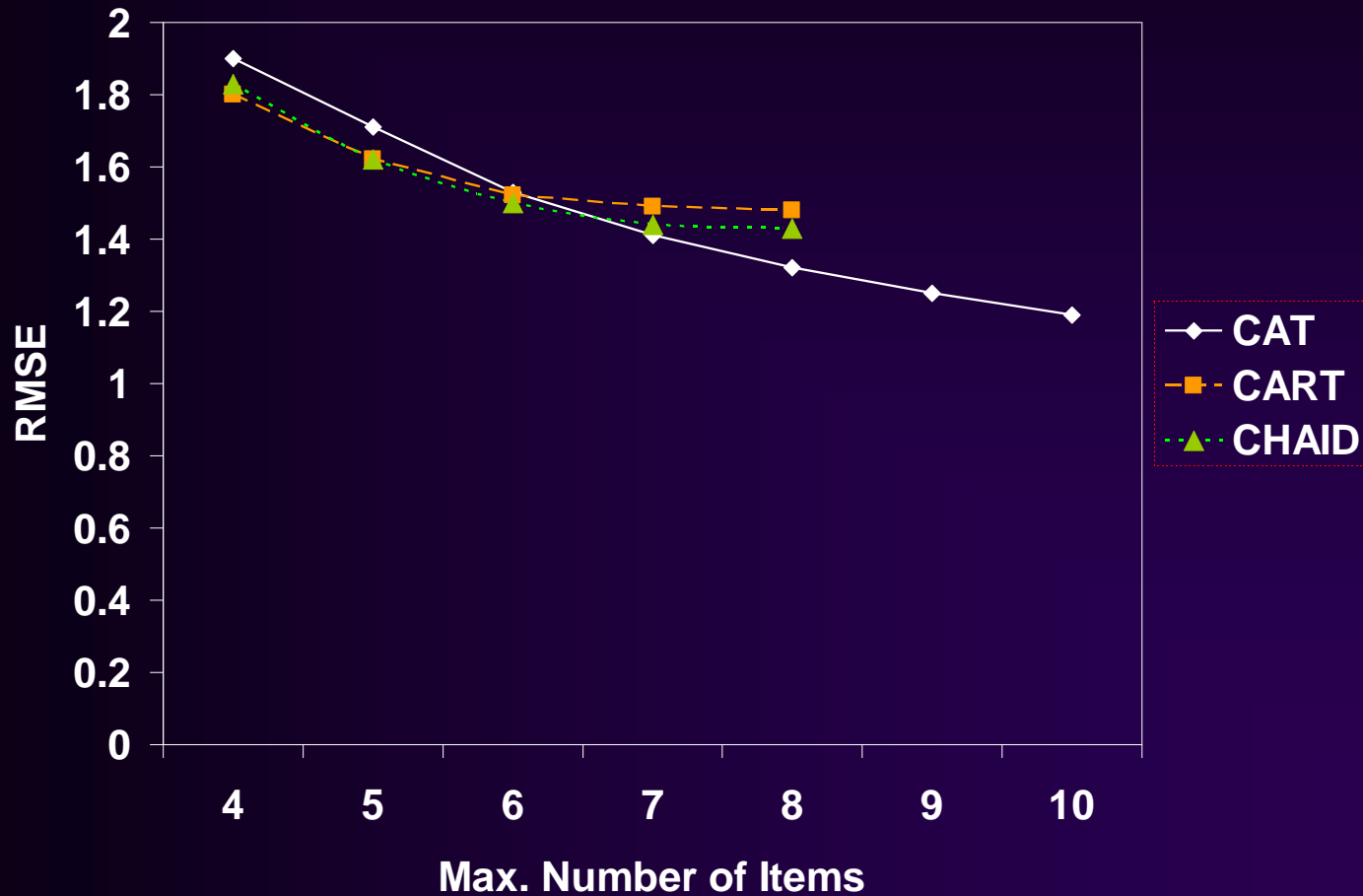
SPSy: Measurement Bias



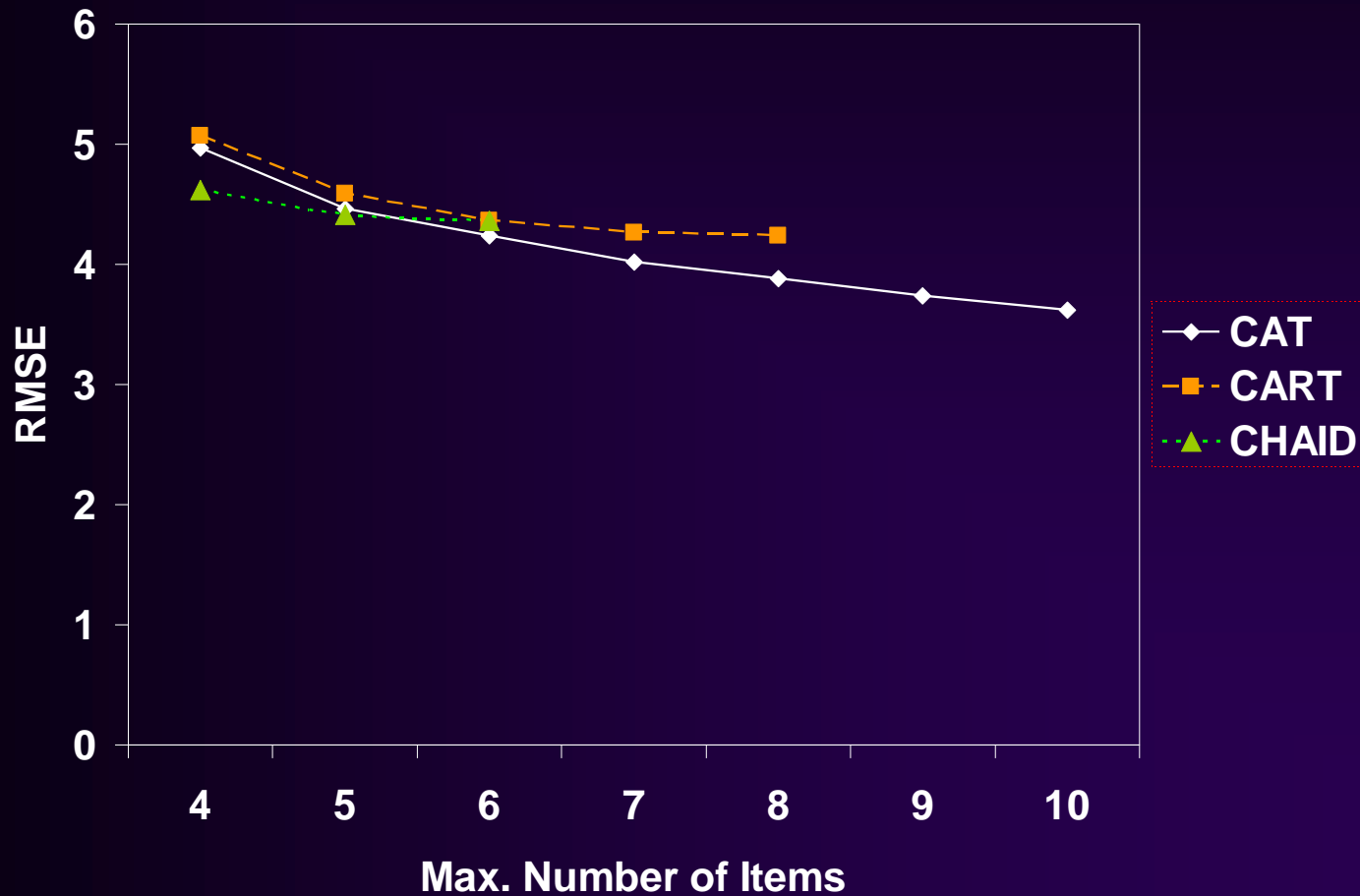
SPSr: Measurement Bias



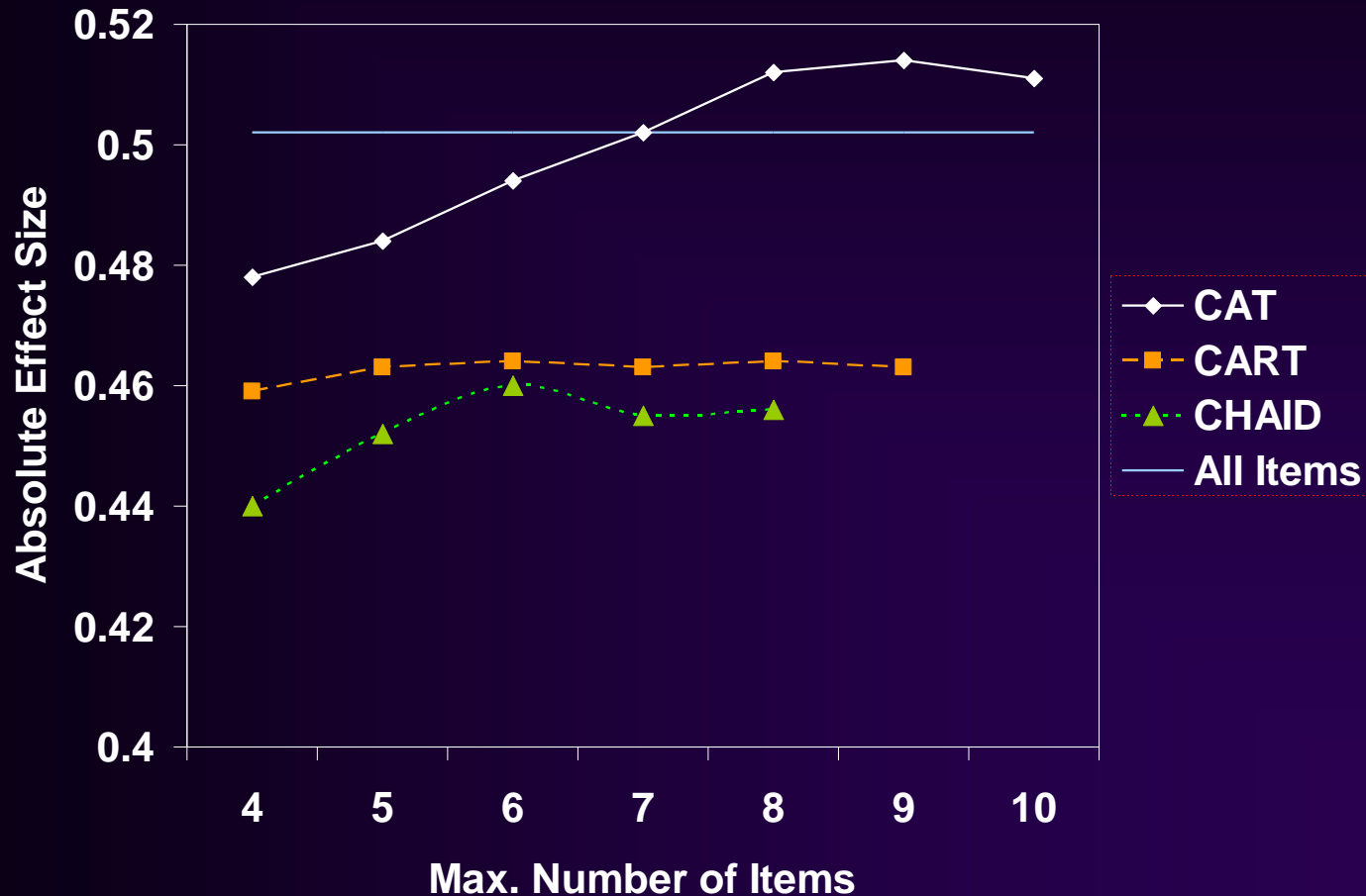
SPSy: RMSE



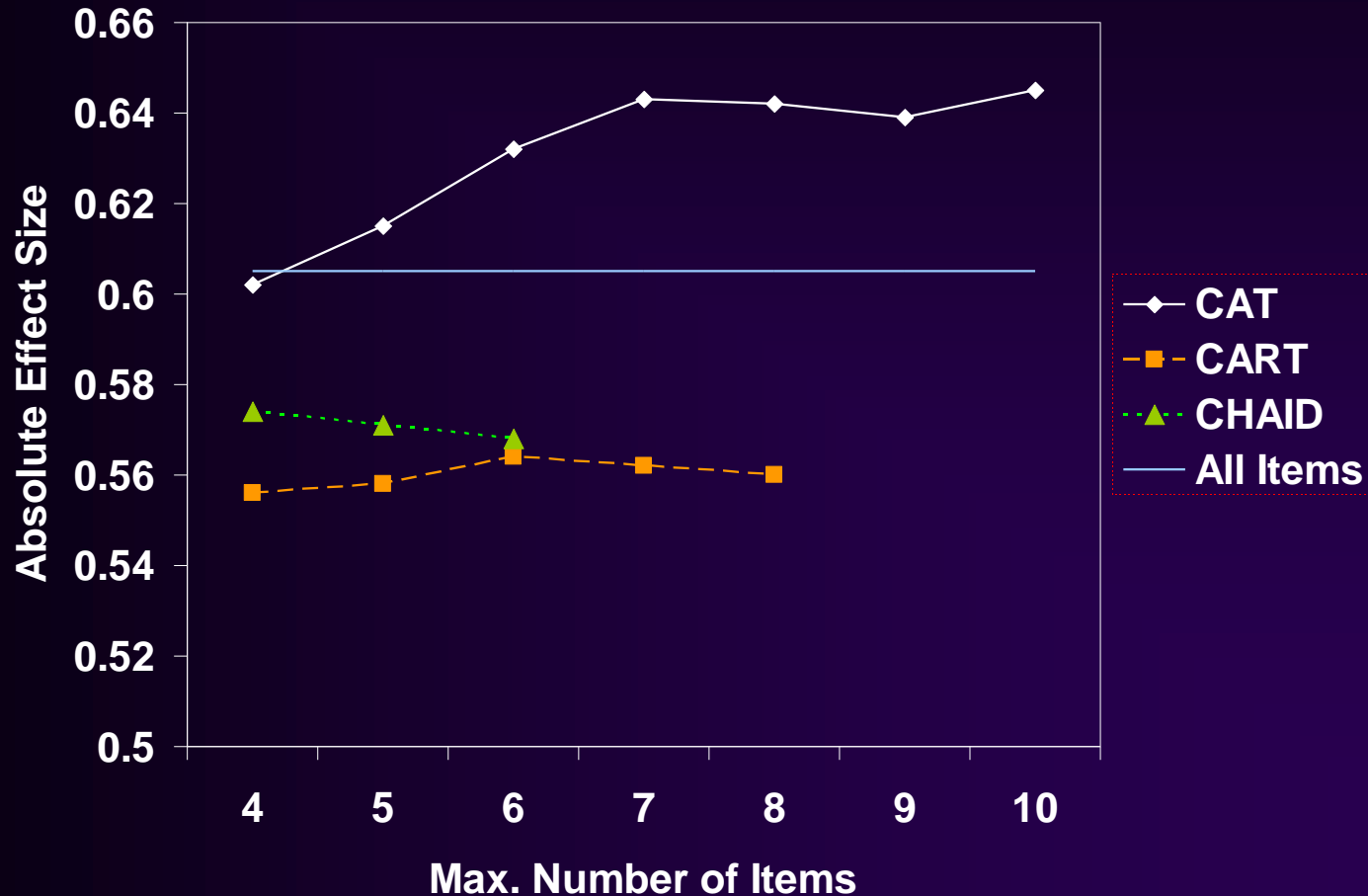
SPSr: RMSE



SPSy: Effect Size



SPSr: Effect Size



Conclusions

- Decision tree methods were more efficient than CAT
 - CART for dichotomous items (SPSy)
 - CHAID for polytomous items (SPSr)
- Score bias was low in all conditions, particularly for decision trees using dichotomous items
- In early stages of administration, decision trees provided slightly higher correlations with the full scale and lower RMSE values.
- But...

Conclusions

- CAT outperformed decision tree methods in later stages of administration.
- CAT also outperformed decision trees with respect to sensitivity to group differences as measured by effect size.

CAT vs. Decision Trees

- CAT selects items based on two criteria:
 - Item location relative to current estimate of theta
 - Item discrimination
- Decision Trees select items that best discriminate between groups defined by the total score.
- **CAT is optimal only when trait level is well estimated.**
- Findings suggest that combining decision tree followed by CAT item selection may be advantageous.

Thank You!

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For psychometric information on the Global
Appraisal of Individual Needs, go to:

<http://www.chestnut.org/li/gain/#GAIN%20Working%20Papers>